Cycling in the Southern Hemisphere

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Abstract

We say a (di) graph is k-traceable if every sub(di)graph of order k is traceable. Clearly a complete graph (tournament) is 2-traceable and a traceable graph is n-traceable. For small k every k-traceable graph is Hamiltonian, but that property does not hold for $k \ge 5$. The Traceability Conjecture (TC) is that every k-traceable graph of order at least 2k - 1 is traceable. Last May I worked with Frick, van Aardt, and Nielson to obtain results concerning the cycle structure of strong k-traceable oriented graphs. In particular we have an upper bound on the order of such graphs.