Abstract: Given a graph G = (V, E), if $e = uv \in E$, then the closed edgeneighborhood of e is denoted by $N[e] = \{u'v' \in E | u' = u \text{ or } v' = v\}$. A function $f : E \to \{-1, 0, 1\}$ is called the minus signed edge domination function (MSEDF) of G if $\sum_{e' \in N[e]} f(e') \ge 1$ for every $e \in E$. The minus signed edge domination number $\gamma_{se}^-(G) = min\{f(E)|f$ is an MSEDF of $G\}$. In this paper, we give the lower bound on the minus signed edge-domination number of graphs. In addition, we characterize all graphs G with $\gamma_{se}^-(G) = |E(G)|$.